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**A COMPUTATIONAL MODEL OF IMPLICIT  
MEMORY CAPTURES DYSLEXICS'  
PERCEPTUAL DEFICITS**

**By**

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# **Title: A computational model of implicit memory captures dyslexics' perceptual deficits**

Abbreviated title: Computational Model of Dyslexia

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1 **Abstract**

2 **Dyslexics are diagnosed for their poor reading skills. Yet they characteristically also suffer**  
3 **from poor verbal memory, and often from poor auditory skills. To date, this combined**  
4 **profile has been accounted for in broad cognitive terms. Here, we hypothesize that the**  
5 **perceptual deficits associated with dyslexia can be understood computationally as a deficit**  
6 **in integrating prior information with noisy observations. To test this hypothesis we**  
7 **analyzed the performance of human participants in an auditory discrimination task using a**  
8 **two-parameter computational model. One parameter captures the internal noise in**  
9 **representing the current event, and the other captures the impact of recently acquired**  
10 **prior information. Our findings show that dyslexics' perceptual deficit can be accounted**  
11 **for by inadequate adjustment of these components; namely, low weighting of their implicit**  
12 **memory of past trials relative to their internal noise. Underweighting the stimulus statistics**  
13 **decreased dyslexics' ability to compensate for noisy observations. ERP measurements (P2**  
14 **component) while participants watched a silent movie, indicated that dyslexics' perceptual**  
15 **deficiency may stem from poor automatic integration of stimulus statistics. Taken together,**  
16 **this study provides the first description of a specific computational deficit associated with**  
17 **dyslexia.**

18

19 **Statement of significance**

20 This study presents the first attempt to specify the mechanisms underlying dyslexics' perceptual  
21 difficulties computationally, by applying a specific model, inspired by the Bayesian framework.

22 This model dissociates between the contribution of sensory noise and that of the prior statistics in  
23 an auditory perceptual decision task. We show that dyslexics cannot compensate for their  
24 perceptual noise by incorporating prior information. In contrast, adequately reading controls'  
25 usage of previous information is like that of an optimal decision maker. We used ERP  
26 measurements to assess the neuronal stage of this deficit. We found that unlike their peers,  
27 dyslexics' ERP responses are not sensitive to the relations between the current observation and  
28 the prior, indicating that they cannot establish a reliable prior.

29

## 30 **Introduction**

31 The controversy surrounding the deficits underlying dyslexics' difficulties is still unresolved.  
32 The prevailing theory claims that dyslexics' phonological representations, whose adequacy is  
33 crucial for efficient usage of the alphabetical code, are impaired (Snowling, 2000). However,  
34 dyslexics perform well on some tasks that rely on phonological representations (reviewed in:  
35 Ramus and Ahissar, 2012). A computationally-motivated imaging study found that dyslexics'  
36 task-specific top-down tuning to phonological processing, as revealed in their thalamic response,  
37 is impaired (Díaz et al., 2012), suggesting that access to phonological representations may be  
38 deficient in dyslexia (e.g. Boets et al., 2013; Ramus, 2014). Nevertheless, other studies have  
39 found that dyslexics' automatic responses to basic sounds are noisier than those of good readers  
40 (e.g. Nagarajan et al., 1999; Hornickel and Kraus, 2013). The anchoring deficit hypothesis  
41 (Ahissar et al., 2006; Ahissar, 2007) states that dyslexics' deficits stem from poor utilization of  
42 stimulus repetitions. In this framework dyslexia does not result from a deficit in stimulus  
43 processing (sensation) or alternatively from a deficit in memory-representation, but from a  
44 deficit in the match between them (similar to the concept of predictive coding; Díaz et al., 2012).

45 The current study was designed to generalize and quantify the impaired-anchoring hypothesis  
46 in a computational model, which specifies the experimental conditions that enhance dyslexics'  
47 difficulties. A 2-tone discrimination task was used because it is simple, quantifiable, and  
48 provides a reliable predictor of performance in phonologically related tasks (children - Mengler  
49 et al., 2005; Banai and Yifat, 2012; Banai and Ahissar, 2013; adults - Amitay et al., 2002;  
50 Oganian and Ahissar, 2012). Previously, we showed that individuals with dyslexia have  
51 difficulties benefitting from simple stimulus repetitions on this task (Ahissar et al., 2006;  
52 Ahissar, 2007; Oganian and Ahissar, 2012). Here we used a version of this task that contains no  
53 repetitions. Instead, it has richer statistics, which allowed us to analyze the impact of stimulus  
54 history on single trials. Specifically, it allowed us to separate the trials in which performance is  
55 expected to “benefit” from stimulus history from those trials in which these statistics are  
56 expected to hamper performance.

57 We utilized an online computational model (Raviv et al., 2012), which quantitatively specifies  
58 the integration of context on the 2-tone discrimination task, to disentangle dyslexics' disabilities.  
59 The model posits that rather than comparing the second tone in each trial to the first one,  
60 listeners compare the frequency of the second tone to a weighted average of the frequency of the  
61 first tone and a memory trace of the frequencies of the tones presented in previous trials. This  
62 may allow listeners to reduce the disruptive effect of noise in the internal representation of the  
63 first tone (e.g., noise added in the retention interval), by combining this noisy representation with  
64 that of previous trials in a way that qualitatively resembles Bayesian reasoning (Lu et al., 1992;  
65 Preuschhof et al., 2010; Ashourian and Loewenstein, 2011). Note, however, that a Bayesian  
66 inference specifies exactly how the prior distribution should be integrated in perception. By  
67 contrast, the prior distribution is not explicitly learned in our model; nor is the extent to which

68 previous trials affect perception in a parameter. Using the model we conclude that dyslexics'  
69 poorer perceptual performance is associated with suboptimal incorporation of prior knowledge in  
70 perception.

71 To further characterize the processes underlying the integration of the stimulus statistics in  
72 perception, we measured ERP responses that are sensitive to stimulus statistics (the P2  
73 component; Tremblay et al., 2001; 2010). Unlike controls', dyslexics' P2 did not show such  
74 sensitivity.

75 Taken together, these results pave the way for a better understanding of dyslexics' perceptual  
76 deficits as a computational impairment related to the learning and incorporation of prior sensory  
77 information.

78

## 79 **Materials and Methods**

### 80 *Participants*

81 Twenty eight native Hebrew speakers (14 dyslexics and 14 good readers), students at the Hebrew  
82 University (mean age = 25.4 years; STD = 2.2; 18 females) were considered in this study.  
83 Recruitment was based on ads at the Hebrew University. Monetary compensation for  
84 participation was according to standard student rates. The study was approved by the Hebrew  
85 University Committee for the Use of Human Subjects in Research. All dyslexic participants  
86 (except one, whose reading, phonological and reasoning profile matched the profile of the other  
87 dyslexic participants) had been diagnosed prior to the study by clinicians using a standard  
88 didactic test approved by the Israeli Ministry of Education. Participants with more than 2 years  
89 of formal musical education were excluded, so that musical training would not be a major  
90 contributor to their pitch sensitivity (Micheyl et al., 2006; Parbery-Clark et al., 2011). Six other

91 participants were excluded from participation based on musical background. Participants with  
92 poor Block Design scores (lower than a normalized score of 7) were also excluded from the  
93 study. Two such additional participants were excluded based on this criterion. All participants  
94 filled in a questionnaire regarding any neurological or psychiatric disorders. None of the  
95 participants reported any disorders.

96

### 97 *Procedure*

98 All participants were administered 3 sessions on three different days:

99 In session 1 participants were administered a series of cognitive assessments.

100 In session 2, ERPs were recorded. Participants watched a silent movie while a series of stimuli  
101 was presented to them.

102 In session 3 the same series of stimuli was presented, and participants actively engaged in the  
103 frequency discrimination task.

104

### 105 *General assessments*

106 General cognitive abilities were assessed on two standard tasks:

107 A. Non-verbal reasoning ability. This was measured with the Block Design, a standard test for  
108 assessing visuo-spatial reasoning (WAIS-III; Wechsler, 1997).

109 B. Short term verbal memory. This was evaluated with the standard Digit Span task (forward  
110 and backward; Hebrew version of WAIS-III; Wechsler, 1997).

111

### 112 *Phonological skills*

113 Phonological skills were assessed using two types of phonological tasks:

114 A. Phonological decoding. Single pseudo-word and real-word reading were assessed using two  
115 standard Hebrew lists designed by Deutsch and Bentin (Deutsch and Bentin, 1996). One list  
116 contains 24 punctuated Hebrew words and the other contains 24 punctuated pseudo-words; i.e.  
117 words with Hebrew morphology but no meaning. Both accuracy and rate were scored.

118 B. Phonological awareness was assessed using the Spoonerism task (MacKay, 1970; Möller et  
119 al., 2007) Participants heard (Hebrew) word pairs and were asked to switch the first phonemes of  
120 the two words and respond vocally (e.g.: /laila tov/ , “good night” in Hebrew, should be switched  
121 to /taila lov/). Both accuracy and rate were scored.

122 We merged accuracy and speed in all phonological tests into a combined phonological score by  
123 averaging the  $z$  score (relative to the control group distribution) within each subject.

124

#### 125 *Stimulation procedure for 2-tone frequency discrimination*

126 Participants were presented with sequences (blocks) of tone pairs (50 ms, 70 dB each tone; 620  
127 ms inter-tone intervals and 1380 ms inter-pair intervals). They were asked to indicate which of  
128 the 2 tones in each pair (i.e. trial) had a higher pitch. No feedback was provided.

129 Participants were presented with a fixed easy-to-difficult sequence of stimuli based on the  
130 average sequence of frequency differences that were given to participants (students, adequate  
131 readers with no, or only minor, musical background) in an adaptive staircase procedure (3-down  
132 1 up) which converges at ~80% correct (Nahum et al., 2010). Consequently, the average  
133 performance was similar in the two protocols. This pseudo-adaptive sequence of tone pairs was  
134 chosen in order to use the same easy-to-difficult sequence of stimuli for all subjects, under both  
135 the passive and active conditions.

136 Each participant performed 700 trials in 2 separate blocks:

137 1. In the *No-Reference* protocol, on each trial, a tone was chosen randomly from 800 Hz to  
138 1,200 Hz. The other tone was determined according to the frequency difference that was pre-  
139 assigned to that trial and could be higher or lower than the randomly chosen tone. The order of  
140 the tones was random. This block consisted of 300 trials. The difference between the two tones  
141 began at 25% and decreased gradually to 18%.

142 2. In the *Reference-Interleaved* condition, one of the tones was 1,000 Hz in all trials (i.e.  
143 Reference tone) and the other tone was determined according to the frequency difference that  
144 was pre-assigned to that trial. The order of the tones was pre-determined: odd number trials -  
145 *Reference 1<sup>st</sup>*; even number trials - *Reference 2<sup>nd</sup>*. This block consisted of 400 trials. The  
146 difference between the two tones began at 25% and decreased gradually to 5-7%. The order of  
147 the blocks was counter-balanced across participants.

148

#### 149 *Parameter estimation of the Implicit Memory Model (IMM)*

150 We modeled the responses made by the participants using the Implicit Memory Model (IMM;  
151 Raviv et al., 2012). According to this model, choices in each trial are determined by the  
152 difference between the frequency of the second tone and a weighted average ( $M_1$ ) of the noisy  
153 memory of present and past frequencies of the first tone. Formally,

$$154 \quad a(t) = \text{sgn}(M_1(t) - f_2(t)) \quad \text{Eq. 1.}$$

155 where  $a(t)$  denotes the choice of the participant on trial  $t$ ,  $\text{sgn}$  is the sign function,  $f_2(t)$  is the  
156 frequency of the second tone on trial  $t$  and:

$$157 \quad M_1(t) = \gamma M_1(t-1) + (1-\gamma)(f_1(t) + z(t)) \quad \text{Eq. 2.}$$

158 where  $f_1(t)$  is the frequency of the first tone on the trial,  $z(t)$  is an independent Gaussian  
159 random variable with zero mean and variance  $\dagger^2$  and we assume resetting of the initial

160 conditions  $M_1(t=1) = f_1(t=1) + z(t=1)$  (Shteingart et al., 2013). This model is characterized by  
 161 two parameters,  $\dagger$  and  $y$ . The first parameter  $\dagger$  denotes the level of internal noise in the  
 162 process of “sensing and memorizing” the first tone on each trial. The second parameter  $y$   
 163 denotes the weight of previously stored stimuli in the current comparison.  
 164 Therefore, the probability to respond “1<sup>st</sup> tone higher” is:

$$165 \quad \Pr["1"] = \Phi\left(\frac{M_1(t) - f_2(t)}{\dagger_e(t)}\right) \quad \text{Eq. 3.}$$

166 where  $\Phi$  is the cumulative normal distribution function and  $\dagger_e(t)$  is the effective response  
 167 variance at trial  $t$ , which depends on  $\dagger$ ,  $y$  and  $t$ :

$$168 \quad \dagger_e = \dagger \sqrt{y^{2t-2} + (1-y^{2t-2}) \frac{1-y}{1+y}} \quad \text{Eq. 4.}$$

169 For each participant, we estimated the two parameters,  $y$  and  $\dagger$  that minimize the squared  
 170 distance between the predicted response probabilities of the model and the observed responses in  
 171 the frequency discrimination task. To assess the reliability of this estimate, we bootstrapped the  
 172 trials for each participant by 1,000 samples of 300 trials with replacement and re-estimating  
 173 parameters.

174 We then estimated the optimal impact of implicit memory given this estimated  $\dagger$ ; i.e., for  
 175 each participant we found  $y^*$  - the  $y$  that would maximize success on the auditory task. We  
 176 defined inadequacy, or sub-optimality, of the implicit memory weighting of each participant as  
 177 the difference between  $y^*$  and the estimated  $y$ .

178

179 *Calculating the optimal y*

180 The optimal  $y$  is defined as the value of  $y$  that minimizes the probability of an error in the  
 181 stimulation schedule for a fixed value of  $\dagger$ .

182 We defined mental difference ( $D(t)$ ) and correct difference ( $C(t)$ ) on each trial as:

183  $D(t) = f_2(t) - M_1(t)$  **Eq. 5.**

184  $C(t) = f_2(t) - f_1(t)$  **Eq. 6.**

185 Thus the probability to make a correct decision on each trial is:

186  $\Pr[\text{correct}] = \Pr[\text{sign}(D(t)) = \text{sign}(C(t))]$  **Eq. 7.**

187 According to Sheppard's Median Dichotomy Theorem (Sheppard, 1899; Kendall et al., 1987  
 188 p.482):

189  $\Pr[\text{sign}(D(t)) = \text{sign}(C(t))] = \frac{1}{2} + \frac{1}{f} \sin^{-1}(\dots_m)$  **Eq. 8.**

190 where:  $\dots_m = \frac{\text{cov}(D, C)}{\sqrt{\text{var}(D) \text{var}(C)}}$  is the correlation between the mental difference and the correct

191 difference.

192 The probability of a correct response is monotonous over  $\dots_m$ ; thus it is sufficient to maximize

193  $\dots_m$  over  $y$  :

194  $\dots_m = \frac{(2-y+(y-2)\dots_f)\dagger_f^2}{\sqrt{\left(\dagger_f^2 + 2\dagger_f^2(y-1)\dots_f + y^2\left(\frac{1-y}{1+y}(\dagger_f^2 + \dagger^2)\right) + (1-y)^2(\dagger_f^2 + \dagger^2)\right)}(2(1-\dots_f)\dagger_f^2)}$  **Eq. 9.**

195 where  $\dots_f = \frac{\text{cov}(f_1, f_2)}{\sqrt{\text{var}(f_1)\text{var}(f_2)}}$  is the correlation between the two tones and  $\dagger_f^2$  is the variance  
 196 of  $f_1$  (the overall variance of the frequencies of the first tones), which is also equivalent to the  
 197 variance of  $f_2$  (the same marginal distributions for the frequencies of the first and the second  
 198 tones).

199 The optimal  $y$  is a solution to the equation:

$$200 \quad \frac{\partial \dots_m}{\partial y} = 0 \quad \text{Eq. 10.}$$

201 Resulting in:

$$202 \quad y^* = \frac{1}{6} \left( \frac{2\dagger_f^2}{\dagger_{f\dots f}^2} + \frac{2^{4/3} \left( \dagger_f^4 (\dots_f - 9) \dots_f - 7\dagger_{f\dots f}^2 \dagger_f^2 + \dagger_f^4 \right)}{\dagger_{f\dots f}^2 A} + \frac{2^{2/3}}{\dagger_{f\dots f}^2} A - 4 \right) \quad \text{Eq. 11.}$$

203 where:

$$204 \quad A = \sqrt[3]{2\dagger_{f\dots f}^6 (27 + \dots_f) + 3\dagger_{f\dots f}^4 (20\dots_f - 9)\dagger_f^2 - 21\dagger_{f\dots f}^2 \dagger_f^4 + 2\dagger_f^6 + 9\dagger_{f\dots f}^2 B} \quad \text{Eq. 12.}$$

$$205 \quad B = \sqrt{(\dagger_f^2 + \dagger_f^2) \left( 4\dagger_{f\dots f}^6 (3 + \dots_f)^2 + 12\dagger_{f\dots f}^4 (1 + 3\dots_f)\dagger_f^2 - 3\dagger_f^2 (1 + 4\dots_f)\dagger_f^4 + \dagger_f^6 \right)} \quad \text{Eq. 13.}$$

206 Since this computation assumes an infinite number of trials, the solution is only an asymptotic  
 207 approximation of the optimal  $y$ . In order to verify its proximity to the optimal  $y$ , with a finite  
 208 number of trials, we ran numerical simulations. We estimated the  $y$  that yielded the highest  
 209 accuracy rate in the actual sequence of trials used in the experiment, for various values of  $\dagger$  and  
 210 compared the two solutions. The numerical and analytical calculations nearly overlapped.

211

212 *ERP recordings and analyses*

213 Electrophysiological activity was recorded in a sound-attenuated room while participants heard  
214 the tone sequences either passively (session 2) or while actively performing the task (session 3).  
215 Sounds were produced using Matlab (The Mathworks inc., Natick, MA) and were presented by  
216 E-Prime 1.1 software (Psychology Software Tools inc., Sharpsburg, PA). The EEG was recorded  
217 from 32 active Ag-AgCl electrodes mounted on an elastic cap using the BioSemi ActiveTwo  
218 tools and recording software (BioSemi B.V., Amsterdam, Netherlands). Electrode sites were  
219 based on the 10-20 system (American Electroencephalographic society, 1991). Two additional  
220 electrodes were placed over the left and right mastoids. Horizontal EOG was recorded from two  
221 electrodes placed at the outer canthi of both eyes. Vertical EOG was recorded from electrodes on  
222 the infraorbital and supraorbital regions of the right eye in line with the pupil.

223 EEG and EOG signals were sampled at 256 Hz, amplified and filtered with an analogue band-  
224 pass filter of 0.16 – 100 Hz. Offline analysis was performed using Brain Vision Analyzer 1.05  
225 software (Brain Products GmbH, Germany). The EEG signal was digitally band-pass filtered  
226 between 1 Hz and 30 Hz to remove large drifts in signal and high frequency noise. ICA analysis  
227 was trained on the entire length of each block to identify components that reflect eye blink or eye  
228 movement evoked electrical activity. An eye related component was identified by its time-  
229 correlation with the occurrence of blinks or saccades. This relationship between the identified  
230 component and eye blink activity was verified by controlling that the component's scalp  
231 distribution was typical of eye-related electrical activity. Data were referenced to the nose  
232 channel to remove external electrical influence. Artifact rejection was applied to the non-  
233 segmented data according to the following criteria: any data point with EOG or EEG  $> \pm 100 \mu\text{V}$   
234 was rejected along with the data  $\pm 300$  ms around it. In addition, if the difference between the

235 maximum and the minimum amplitudes of two data points within an interval of 50 ms exceeded  
236 100  $\mu$ V, data  $\pm$  200 ms around it were rejected. Finally, if the difference between two adjacent  
237 data points was more than 50  $\mu$ V, the data  $\pm$  300 ms around it were rejected. Trials containing  
238 rejected data points were omitted from further analysis (average omission of 17 trials per  
239 subject).

240 For ERP averaging across trials, the EEG was parsed to 2,000 ms epochs starting 500 ms  
241 before the onset of the first stimulus in each pair, and averaged separately for each electrode. The  
242 baseline was adjusted by subtracting the mean amplitude of the pre-stimulus period (500-150 ms  
243 before the onset of the first stimulus in the trial) of each ERP from each data point in the epoch.  
244 The pre-stimulus baseline period was calculated from this time interval to exclude effects of  
245 anticipatory responses that precede informative anticipated stimuli (CNV; Walter et al., 1964).

246 ERP analysis was based on the epochs that were recorded with electrode Cz (at the vertex of  
247 the scalp) after they were processed as described above. This electrode measured the most  
248 prominent response to the auditory stimuli. Each participant's data (accumulated during the two  
249 blocks) were analyzed separately.

250

## 251 **Results**

### 252 *Participants' cognitive profile*

253 Dyslexics' performance did not differ from controls' performance on general reasoning skills as  
254 measured by the Block Design (Snowling, 2000). However, as expected, their performance was  
255 poorer than the controls' on the measures of verbal memory and phonological skills (see Table  
256 1). All the dyslexic participants were poorer decoders than all the control participants.  
257 Specifically, the combined phonological score (average z scores across all phonological tasks) of

258 the best reader in the dyslexic group was 0.3 standard deviations lower than that of the poorest  
 259 reader in the control group.

260 **Table 1. Participants' general cognitive and phonological skills**

Test	Control (STD) N=14	Dyslexic (STD) N=14	Mann-Whitney z value
<b>General cognitive</b>			
Block Design Norm	12.4 (2.3)	10.8 (2.3)	1.7
Digit Span Norm	11.6 (3.4)	7.4 (2.2)	3.2 **
<b>Phonological Decoding Speed [items/minute]</b>			
Single-word Reading Rate	104.5 (33.1)	62.7 (18.4)	3.5 ***
Pseudo-word Reading Rate	59.7 (16.4)	29.4 (9)	4.3 ***
<b>Phonological Decoding Accuracy [fraction correct]</b>			
Single-word Reading Accuracy	1 (0)	0.9 (0.1)	3.7 ***
Pseudo-word Reading Accuracy	0.9 (0.1)	0.6 (0.2)	4 ***
<b>Phonological Awareness</b>			
Spoonerism Rate [items/minute]	10.9 (4)	5.1 (2)	3.7 ***
Spoonerism Accuracy [fraction correct]	0.9 (0.1)	0.7 (0.3)	2.6 **

261 \*\*\* $P < 0.01$ , \*\*\*\* $P < 0.001$

262

263 *The effect of the stimulus statistics on performance in Frequency Discrimination*

264 In order to evaluate the impact of the stimulus statistics on perception parametrically, we used  
 265 the two-tone frequency discrimination task. On each trial, participants are presented with two

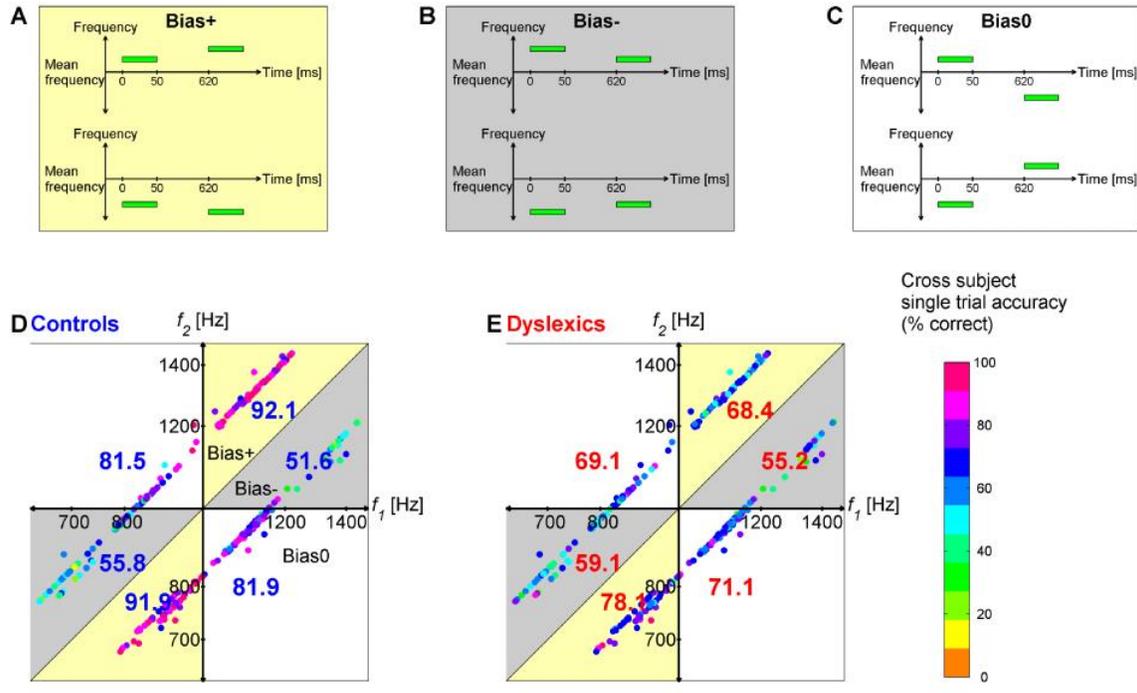
266 sequentially-presented pure tones and are instructed to indicate which had a higher pitch (Figs.  
267 1A-1C, see also Materials and Methods). The frequencies of the two stimuli were drawn from a  
268 broad distribution, a protocol we denoted as *No-Reference* protocol. Though frequency  
269 discrimination tasks are traditionally used as an assessment of low-level sensory bottlenecks, we  
270 have shown that in this (*No-Reference*) protocol, which is devoid of a repeating standard tone,  
271 performance is substantially affected by the statistics of previous trials (Raviv et al., 2012).  
272 When the two tones are higher than the average, performance has been shown to be better when  
273 the second tone is higher than the first. Similarly, when the two tones are lower than the average,  
274 findings have indicated that performance is better when the second tone is also lower than the  
275 first (Romo et al., 2002; Hairston and Nagarajan, 2007; Alcalá-Quintana and Garcí'a-Pérez,  
276 2011; Raviv et al., 2012). This result can be understood in a Bayesian framework where  
277 participants utilize prior information about the distribution of frequencies to compensate for  
278 noise in the representation of the memorized tone. Loosely speaking, this computation results in  
279 a “contraction” of the representation of the first tone to the mean frequency in the experiment.

280 Based on these findings, we divided the trials according to the sign of the predicted  
281 contribution of the statistics of the experiment to the trial. Specifically, we divided the trials into  
282 three types, based on their relationship to the mean frequency. *Bias+* trials were defined as those  
283 trials in which the experiment's statistics was predicted to improve performance. Namely, (1) the  
284 frequencies of the two tones were either both higher than the mean frequency or both lower than  
285 the mean frequency and (2) the frequency of the second tone was more extreme than that of the  
286 first tone (higher when the 2 tones were above average and lower when they were below  
287 average; Fig. 1A; yellow zones in Figs. 1D and 1E). In these trials the contraction of the first tone  
288 towards the mean increases its perceived difference from the second tone, and was expected to

289 improve performance. By contrast, *Bias-* trials were trials in which the statistics was predicted to  
290 hamper performance. Namely, when the two tones were above the average, the second tone was  
291 lower than the first and when they were lower than the average, the second tone was higher than  
292 the first (Fig. 1B; gray zones in Figs. 1D and 1E). In these trials, contracting the first tone  
293 towards the mean frequency decreased its perceived difference from the second tone and was  
294 expected to be detrimental to performance. *Bias0* trials (Fig. 1C; white zones in Figs. 1D and 1E)  
295 were trials in which the first and the second tone flanked the mean frequency.

296 In line with a previous study (Raviv et al., 2012), we found that trial type had a marked effect  
297 on the ability of controls to discriminate the two tones. The probability that controls would  
298 correctly discriminate the frequencies of the two stimuli in the *Bias+*, *Bias0* and *Bias-* regions  
299 spanned a broad range of 92%, 81.8% and 54.9%, respectively. This was found despite the fact  
300 that that the experiment was designed in a way that there was no difference in the “objective”  
301 difficulty of the three regions (quantified as the absolute difference between the frequencies of  
302 the two tones on a logarithmic scale depicted as the distance of the points from the diagonal in  
303 Figs. 1D and 1E). When quantifying performance in terms of  $d'$ , we found that the median  $d'$   
304 was significantly better in the *Bias+* regions than in the *Bias0* regions (Median (inter-quartile  
305 range; IQR), *Bias+*  $d'$ : 3.2 (2); *Bias0*  $d'$ : 2 (1.9); Wilcoxon test,  $P < 0.005$ ) and was significantly  
306 better in the *Bias0* regions compared with the *Bias-* regions (*Bias-*  $d'$ : 0 (2.4); Wilcoxon test,  $P <$   
307 0.001). In fact, the control group's performance in the *Bias-* regions was not significantly  
308 different from chance (Wilcoxon test,  $P = 0.55$ ).

309



310

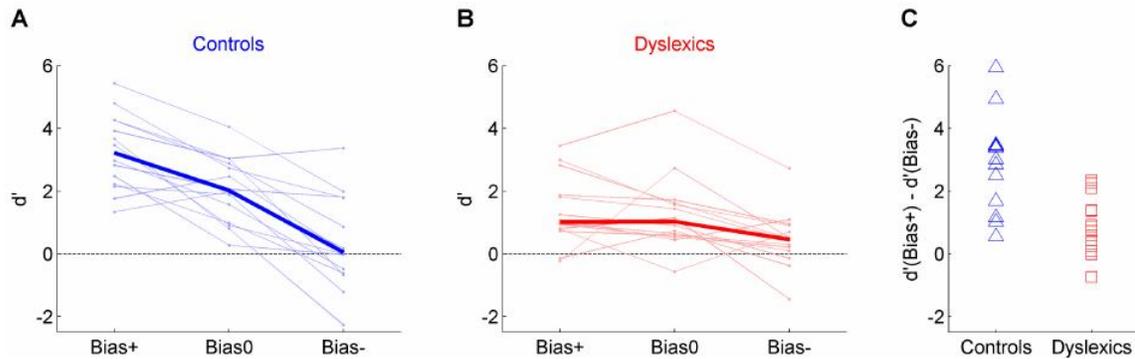
311 **Figure 1.** Performance of controls and dyslexics differentially depend on trial type. . A-C,  
 312 Schematic examples of the three types of trials. (A) in *Bias+* trials the first tone is closer to the  
 313 mean. (B) in *Bias-* trials the first tone is farther from the mean. (C) in *Bias0* trials the two tones  
 314 flank the mean . D-E, Mean performance (% correct) of controls (D) and dyslexics (E) in the six  
 315 sub-regions of trial types, plotted on the frequency plane of the second tone  $f_2$  as a function of  
 316 the first tone  $f_1$ . *Bias+* zones (denoted in yellow) are above the diagonal when both tones are  
 317 above the mean frequency (second tone is higher) and below the diagonal when both tones are  
 318 below the mean frequency (second tone is lower). *Bias-* regions (denoted in gray) are  
 319 complementary with respect to the diagonal, and *Bias0* trials (denoted in white) are those trials  
 320 associated with the 2 remaining quarters. Each dot denotes  $f_1$  and  $f_2$  of a trial (tested across  
 321 individuals). The color of each dot denotes the cross-subject average performance for that pair of  
 322 stimuli. Numbers denote the average percent correct in each region.

323

324 By contrast, dyslexics' performance in the *Bias-* region was significantly above chance (58.2%  
325 Wilcoxon test,  $P < 0.05$ ), whereas their accuracy in the *Bias+* regions was lower than that of the  
326 controls (72.4%). Their performance in the *Bias0* region was intermediate (70.7%). When  
327 quantifying their performance in terms of  $d'$ , their median  $d'$  was not significantly better in the  
328 *Bias+* regions than in the *Bias0* regions (Median (IQR), *Bias+*  $d'$ : 1 (1); *Bias0*  $d'$ : 1 (1);  
329 Wilcoxon test,  $P = 0.36$ ), though it was significantly better in the *Bias0* regions than in the *Bias-*  
330 regions (*Bias-*  $d'$ : 0.5 (0.8); Wilcoxon test,  $P < 0.02$ ).

331 To test whether dyslexics' sensitivity to trial type was significantly less than that of the  
332 controls, we assessed the performance of each participant individually. This is illustrated in Fig.  
333 2, where the value of  $d'$  of each participant in each region (*Bias+*, *Bias0* and *Bias-*) is plotted for  
334 all participants (Fig. 2A Controls; Fig. 2B dyslexics). To quantify the sensitivity to the prior  
335 distribution we computed the difference between the values of  $d'$  in the *Bias+* and *Bias-* regions  
336 for each participant (Fig. 2C). Overall, dyslexics' sensitivity, as measured by this difference, was  
337 significantly smaller than controls' (Mann-Whitney test for Condition (*Bias+* vs. *Bias-*) X Group  
338 (controls vs. dyslexics) interaction:  $z = 3.5$ ,  $P < 0.001$ ). These results further indicate that  
339 dyslexics were less influenced by the statistics of the experiment than controls. Note that  
340 dyslexics', (but not controls') performance was significantly above chance level even in the  
341 *Bias-* region, indicating that their reduced sensitivity to the prior distribution did not stem from a  
342 "floor effect". That is, dyslexics' overall poorer performance cannot account for the smaller  
343 difference between their performance on the *Bias+* and *Bias-* trials, since they performed better  
344 than chance in the *Bias-* region.

345



346

347 **Figure 2.** Individual  $d'$ 's in the 3 regions, showing their sensitivity to the stimulus statistics. **A-B**

348 Performance ( $d'$ ) of (A) controls ( $N=14$ ) and (B) dyslexics ( $N=14$ ) in *Bias+*, *Bias0* and *Bias-*

349 trials. Thick lines denote medians. Thin lines denote individual performance. (C) Difference

350 between *Bias+*  $d'$  and *Bias-*  $d'$  for each participant (controls in blue and dyslexics in red). In both

351 groups, performance in the *Bias+* regions was generally better than in the *Bias-* region ( $d'$  of

352 *Bias+* >  $d'$  of *Bias0* >  $d'$  of *Bias-*; Friedman tests, controls:  $P < 0.00005$ ; dyslexics:  $P < 0.005$ ).

353 But controls were more sensitive to the prior distribution than dyslexics (Group X Condition

354 interaction; Mann-Whitney test for interaction of *Bias+* vs. *Bias-* and controls vs. dyslexics,  $z =$

355 3.5,  $P < 0.001$ ).

356

### 357 *Modelling the effect of statistics with the Implicit Memory Model (IMM)*

358 The division of the trials into *Bias+*, *Bias-* and *Bias0* drew on the Bayesian framework, which

359 specifies how performance in a noisy system can benefit maximally from accumulating

360 environmental statistics and incorporating it into its decision-making. As shown above, human

361 performers utilize such statistics even in simple two-tone discriminations. Nevertheless, this

362 incorporation of the statistics deviates from the predictions of an optimal Bayesian performer

363 (Raviv et al., 2012). To quantify listeners' performance, we used a simplified model (the implicit

364 memory model; IMM), in which listeners do not know the full distribution of the stimulus  
365 statistics. Rather, they weigh past trials using an exponentially decaying function (Raviv et al.,  
366 2012).

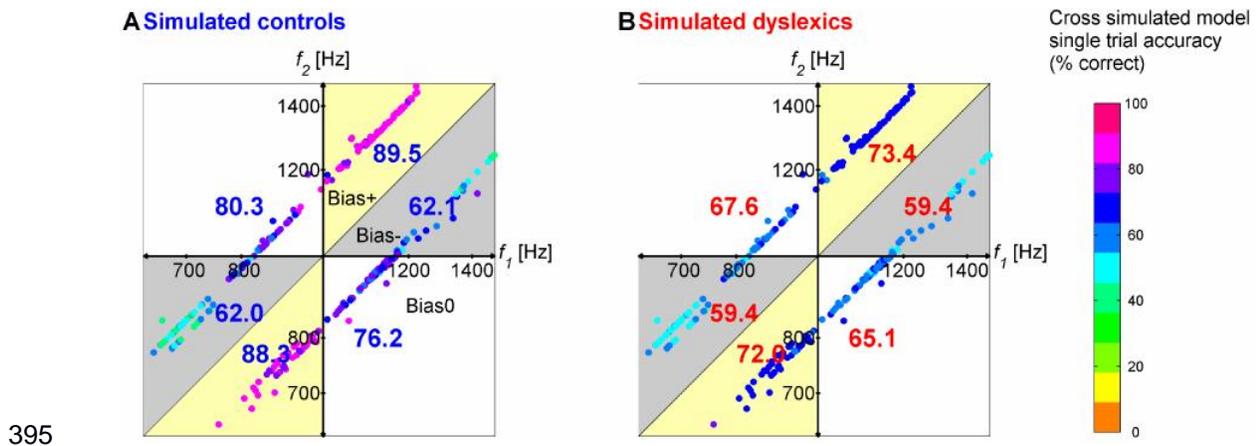
367 The model (Eq. 2 in Materials and Methods) is characterized by two parameters:  $\gamma$  - the  
368 contribution of previous trials ( $\gamma = 0$  - no contribution; the larger the value of  $\gamma$ , the larger the  
369 contribution), and  $\tau$  - the level of internal noise (on a scale of percent difference between the  
370 two tones: the larger the value of  $\tau$  the noisier the within-trial representation). We used the  
371 IMM to estimate the values of  $\gamma$  and  $\tau$  for each participant. We tested the model by simulating  
372 it on the same task using the estimated parameters. Qualitatively, the differential performance in  
373 the three trial types and the different performance level of dyslexics and controls was captured  
374 by the model (Fig. 3). Quantitatively, the difference in performance between the *Bias+* and *Bias-*  
375 regions was slightly larger in the experiment than in the model, in particular for the control  
376 participants.

377 One prediction of the Bayesian framework is that the effect of the stimulus statistics on  
378 behavior should increase when the level of internal noise increases. Qualitatively, this prediction  
379 is intuitive. If the representation of the stimuli is noiseless, performance cannot be improved by  
380 incorporating prior information. However, if the representation of a stimulus is noisy, prior  
381 information would be useful, and the noisier the representation, the larger the weight that should  
382 be given to this prior in the discrimination task. One study in fact showed that in the visual  
383 modality, increasing the level of internal noise enhanced the contribution of prior knowledge to  
384 perception and decision making (Ashourian and Loewenstein, 2011).

385 The IMM model makes no assumptions regarding the relationships between participants'  $\gamma$   
386 and  $\tau$ . Nevertheless the model can be used to determine the extent to which participants'

387 weighting of previous trials (their  $\gamma$ ) was close to optimal given their within-trial noise ( $\dagger$ ) and  
 388 the stimulus statistics (in the sense of maximizing their success rate; *Fig. 4A, green*).

389 Analysis of the parameters characterizing our participants indicated that on average, the  
 390 estimated value of  $\dagger$  was higher among the dyslexic participants (Median (IQR), controls:  $\dagger =$   
 391 35 (40) %; dyslexics:  $\dagger = 98$  (213) %; Mann-Whitney test,  $z = 2.2$ ,  $P < 0.05$ ). Given their higher  
 392  $\dagger$ , the optimal model solution predicted that the dyslexics'  $\gamma$  should also be higher than the  
 393 control's  $\gamma$ . However, the dyslexics'  $\gamma$  was similar to that of the controls (Median (IQR),  
 394 controls:  $\gamma = 0.52$  (0.5); dyslexics:  $\gamma = 0.41$  (0.53); Mann-Whitney test, *n.s.*).

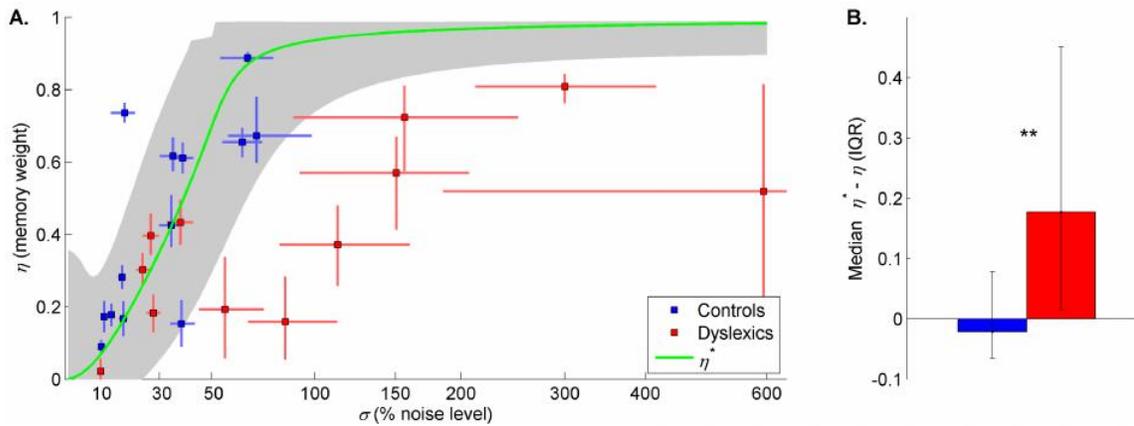


396 **Figure 3.** Simulating the experiment with the IMM model produces similar results to those  
 397 measured experimentally (shown in Figure 1). **A-B**, Mean performance (% correct) of simulated  
 398 controls (**A**) and simulated dyslexics (**B**) in the six sub-regions of trial types plotted on the  
 399  $[f_1, f_2]$  plane. *Bias+* zones are denoted in yellow, *Bias-* in gray and *Bias0* in white. Each dot  
 400 denotes  $f_1$  and  $f_2$  of a trial (tested across simulated individuals). The color of each dot denotes  
 401 the average cross-simulation performance for that pair of stimuli. Numbers correspond to the  
 402 percent correct in each region.

403

404 As shown in Fig. 4A, controls'  $\gamma$ -s (blue squares) were nearly optimal (green line) given their  
405  $\dagger$ -s, indicating that their weighting of the history was similar to that of an "ideal listener" (in the  
406 framework of the IMM). By contrast, dyslexics'  $\gamma$ -s were lower than expected given their  $\dagger$ -s  
407 (red squares). To quantify this group difference, we calculated the difference between the  
408 optimal and the actual  $\gamma$  for each participant. We found that dyslexics' under-weighting of  
409 implicit memory was significantly larger than controls' (Fig. 4B; Mann-Whitney test,  $z = 2.6$ ,  $P$   
410  $< 0.01$ ). Hence, given their internal noise level, Dyslexics, in contrast to Controls, do not give  
411 sufficient weight to prior information.

412 Note that our simple, 2 parameter IMM model only assumes within-trial noise. Hence the  
413 dyslexics' underweighting of the stimulus statistics was suboptimal. An alternative account  
414 would posit that dyslexics' memory is noisy. However, introducing this to the model would  
415 require the addition of a third parameter, whereas our model accounts well for controls'  
416 performance. On the other hand, we could assume optimal weighting of the history (i.e. the  
417 weighting of the history is determined by the stimulus statistics) and replace ( $\gamma$ ) with a  
418 parameter that estimates the noise of previous trials (memory noise). However, this would  
419 require an additional optimality assumption, which for this reason we did not pursue.



420

421 **Figure 4.** Estimated parameters of the Implicit Memory Model for Controls and Dyslexics. **A.**  
 422 Estimated values of  $\eta$  (which determine the proportion of implicit memory in the current  
 423 representation of  $f_1$ ) as a function of the estimated values of  $\sigma$  (percentage of internal noise with  
 424 respect to the difference between the tones within the trial) of controls (blue; error bars denote  
 425 bootstrapped inter-quartile range) and dyslexics (red). For all values of  $\sigma$  the optimal value of  $\eta$   
 426 (the value of  $\eta$  that minimizes the probability of an error in the experiment), denoted as  $\eta^*$ , is  
 427 plotted in green. Gray area depicts the values of  $\eta$  that yield more than 97.5% of the optimal  
 428 performance. **B.** Median of the deviations from optimal weighting of previous trials. Dyslexics'  
 429 deviation was significantly larger than controls' (Mann-Whitney test,  $z = 2.5$ ,  $P < 0.01$ ). Error  
 430 bars denote inter-quartile range.

431

432 Taken together, the findings show that in the framework of IMM, controls' weighting of past  
 433 events was nearly optimal. By contrast, dyslexics' weighting of these past events was too low,  
 434 indicating a deficit in adequate incorporation of prior knowledge into perception.

435

436

437 *ERP results*

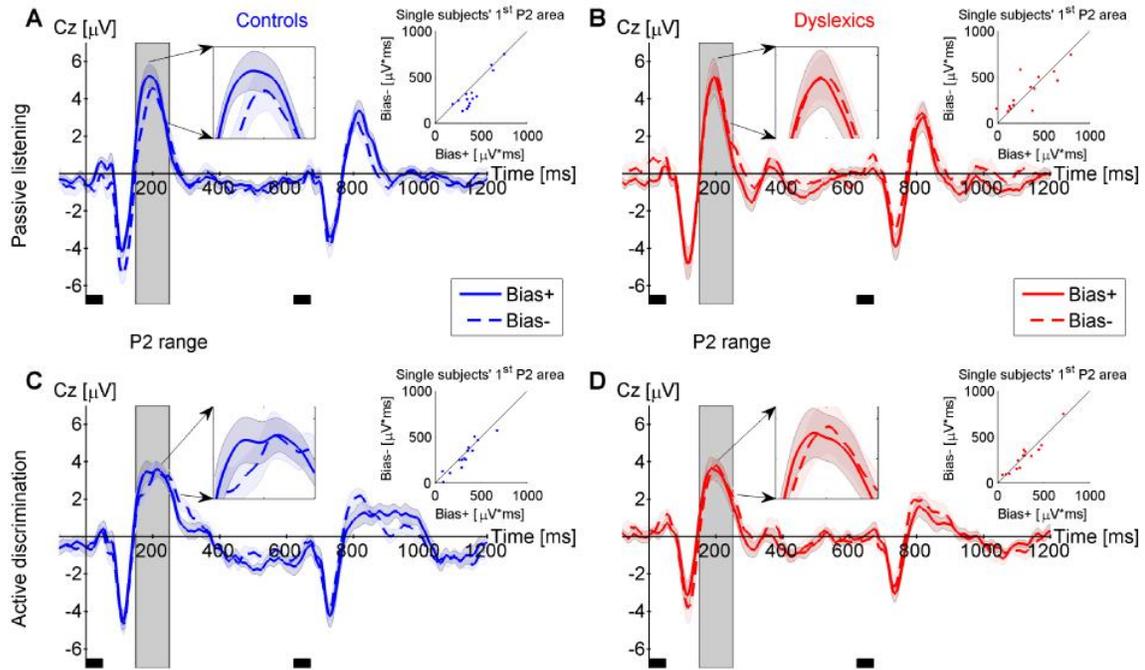
438 The IMM model posits that in the 2-tone discrimination task, the listener compares the frequency  
439 of the second tone to a linear combination of the frequencies of the first tone in the current and  
440 previous trials. This suggests a process in which the comparison is preceded by the formation of  
441 a combined representation. We hypothesized that if dyslexics' reduced weighting of previous  
442 trials stems from an impaired formation of an integrated representation, reduced sensitivity to  
443 stimulus statistics may be apparent even before the second tone is presented. To test this  
444 hypothesis, we measured Event Related Potentials (ERPs). We focused on the dynamics and  
445 magnitude of the P2 component, which is an automatic response evoked by the auditory cortex  
446 (Sheehan et al., 2005; Mayhew et al., 2010). Previous studies, utilizing both oddball (MMN)  
447 (Haenschel et al., 2005; Baldeweg, 2007; Tong et al., 2009) and discrimination paradigms  
448 (Tremblay et al., 2001, 2010; Ross and Tremblay, 2009) have shown that the magnitude of this  
449 component increases with stimulus repetitions, suggesting that this component is sensitive to the  
450 statistics of the experiment. We hypothesized that P2's sensitivity to stimulus repetitions is a  
451 special case of its analog sensitivity to the congruency between the current stimulus and the prior  
452 distribution. Therefore, we predicted that the magnitude of the control's P2 would be larger in  
453 *Bias+* trials than in *Bias-* trials, since the average distance of the first tone from the mean  
454 frequency was smaller in the *Bias+* trials than in the *Bias-* trials (as shown in Figs. 1A and 1B).  
455 Consequently, the first tone in the *Bias+* trials was more congruent with the prior than the first  
456 tone in the *Bias-* trials. We further predicted that dyslexics' P2 would not be as sensitive to trial  
457 type.

458 We recorded ERPs under both passive and active conditions in separate sessions. In the passive  
459 condition, the same series of stimuli was presented to the participants while they were watching a

460 silent movie and were not asked to perform any task. For each participant in each of the specified  
461 trial types, we calculated the area under the curve between 150 ms and 250 ms after the first  
462 tone's onset as his/her individual P2 area. As predicted, we found that the controls' evoked  
463 response (Fig. 5A) was sensitive to the trial type. This was visible in the P2 component of the  
464 response to the first tone. In the *Bias+* trials, this response was, on average, significantly larger  
465 than the response to the first tone of the *Bias-* trials (Wilcoxon test,  $P < 0.005$ ). However, the  
466 dyslexics' P2 was not sensitive to trial type (Fig. 5B; Wilcoxon tests,  $P = 0.46$ ). The difference  
467 between controls' and dyslexics' P2 sensitivity to trial type was also significant (Group X  
468 Condition interaction; Mann-Whitney test,  $z = 2.5$ ,  $P < 0.05$ ). We repeated this analysis when  
469 participants were asked to actively perform the task with the same stimuli, and found similar  
470 results. controls' P2 was sensitive to the trial type (Fig. 5C; Wilcoxon test,  $P < 0.05$ ), though the  
471 magnitude of this effect was smaller than in the passive condition (perhaps due to masking by  
472 additional active components). Dyslexics' P2 did not significantly differ between the two trial  
473 types (Fig. 5D; Wilcoxon tests,  $P = 0.67$ ). In this condition, the interaction was not significant  
474 (Condition X Group; Mann-Whitney test,  $z = 1.2$ ,  $P = 0.22$ ). Taken together, these results  
475 support the hypothesis that dyslexics' computational deficit is associated with a failure to  
476 reliably integrate their on-line representation with the prior distribution.

477 In principle, we expected that individuals' P2 sensitivity to the stimulus statistics would be  
478 correlated with their weighting of previous trials ( $y$ ). This correlation is expected both if P2  
479 reflects the result of the process of incorporation of previous trials into current memory (IMM),  
480 thus directly reflecting the magnitude of the contribution of previous trials, and if it measures the  
481 reliability of the memory trace, which is not captured in the simple IMM model. However, as  
482 shown in Figure 5 (*top right insets*, single subject distribution), while at the group level the

483 difference in P2 sensitivity was very consistent, the magnitude of P2 sensitivity to stimulus  
 484 statistics was too small (in terms of signal to noise ratio) to enable a reliable calculation of these  
 485 correlations.



486

487 **Figure 5.** Grand average ERP measures for the *Bias+* and *Bias-* trial types (electrode Cz). **A, C**  
 488 controls (blue lines). **B, D** dyslexics (red lines). *Bias+* trials are denoted by solid lines and *Bias-*  
 489 trials by dashed lines. In controls, the area of P2 after the first tone (from 150 ms to 250 ms,  
 490 denoted by the gray rectangles) was significantly different between *Bias+* and *Bias-* trial types,  
 491 in both Passive Listening (**A**) and during Active Discrimination (**C**; Wilcoxon tests, Passive:  $P <$   
 492 0.005; Active:  $P <$  0.05). Dyslexics' evoked responses did not differ between the two trial types  
 493 (Wilcoxon tests, **B** Passive:  $P = 0.46$ ; **D** Active:  $P = 0.67$ ). Controls' P2 to *Bias0* trials were in  
 494 between the *Bias+* and *Bias-* responses and are not shown for clarity. Filled areas around the  
 495 mean response denote cross-subject SEM. Small black rectangles under the plots denote the  
 496 temporal location of the two tones in the trial. *Insets*: middle of each plot - P2 region enlarged;

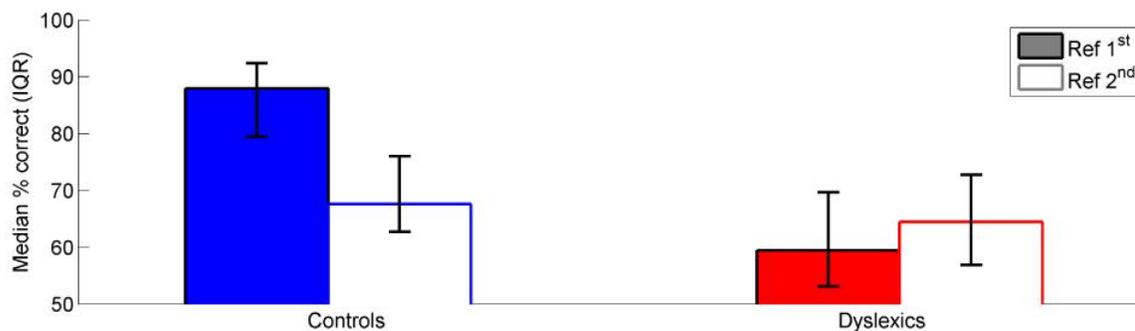
497 top right of each plot - single subject data of *Bias-* versus *Bias+* trials. In the Passive condition  
498 the difference between the trial types was significantly larger among controls than among  
499 dyslexics (Condition X Group interaction; Mann-Whitney test for interaction of *Bias+* vs. *Bias-*  
500 and controls vs. dyslexics,  $z = 2.5$ ,  $P < 0.05$ ).

501

### 502 *Dyslexics' insensitivity to stimulus statistics in a protocol with a reference*

503 Dyslexics' reduced sensitivity to stimulus statistics leads to non-intuitive predictions on specific  
504 trials that should be more challenging for them in other protocols with more structured statistics.  
505 We examined the interleaved reference protocol (Nahum et al., 2010). In this protocol, a  
506 reference (1000Hz) tone is presented on every trial. However, on odd trials it is presented first  
507 (*Ref 1<sup>st</sup>*), whereas on even trials it is presented second (*Ref 2<sup>nd</sup>*). Intuitively (and consistent with  
508 the anchoring deficit hypothesis), dyslexics' performance is expected to be impaired in both,  
509 since both types of trials contain a repeated reference. However, the rationale behind the IMM  
510 model prompts a specific prediction with respect to different trial types, since previous trials are  
511 specifically integrated into the representation of the first tone on each trial. It therefore predicts  
512 that controls should benefit substantially from previous statistics in *Ref 1<sup>st</sup>* trials. In these trials,  
513 integrating previous statistics reduces the noisiness of the representation of the first tone without  
514 modifying its mean. By contrast, in *Ref 2<sup>nd</sup>* trials, the second tone is (approximately) equal to the  
515 mean of the distribution. Therefore, the incorporation of the prior (roughly the mean) to the  
516 representation of the first tone in the same manner decreases the perceived difference, and  
517 hampers performance. If dyslexics' sensitivity to the statistics of the experiment is indeed  
518 reduced, the difference between their performance on the two trial types should be significantly  
519 smaller than that of controls.

520 To test this prediction, all participants performed this interleaved protocol. In line with the  
 521 IMM prediction, and consistent with previous observations (Nahum et al. 2010; see also Romo  
 522 and Salinas, 2003), we found that the performance of controls on *Ref 1<sup>st</sup>* trials was substantially  
 523 and significantly better than their performance on the *Ref 2<sup>nd</sup>* trials (Fig. 6 blue; *Ref 1<sup>st</sup>*: mean  
 524  $86\% \pm 2\%$  SEM correct; *Ref 2<sup>nd</sup>*:  $69\% \pm 4\%$  correct; Wilcoxon test,  $P < 0.001$ ). By contrast, in  
 525 line with IMM's prediction, dyslexics' performance did not differ between these trial types (Fig.  
 526 6 red; *Ref 1<sup>st</sup>*:  $64 \pm 4\%$  correct; *Ref 2<sup>nd</sup>*:  $66 \pm 4\%$  correct; Wilcoxon test,  $P = 0.71$ ). The group  
 527 difference in sensitivity to trial types was also significant (Condition X Group interaction; Mann-  
 528 Whitney test for interaction between Reference position and group,  $z = 3$ ,  $P < 0.005$ ).  
 529



530  
 531 **Figure 6.** Performance on the 2-tone discrimination task using a protocol with a reference  
 532 frequency (1000Hz) presenting the 1<sup>st</sup> and 2<sup>nd</sup> tone in an interleaved manner across trials.  
 533 Performance in trials in which the reference was presented first (*Ref 1<sup>st</sup>*, filled bars) and in trials  
 534 in which the reference was presented second (*Ref 2<sup>nd</sup>*; empty bars). Bars denote the median of  
 535 participants' percent correct. Error bars denote inter-quartile range. controls' performance was  
 536 more affected by the reference than dyslexics' performance (Condition X Group interaction;  
 537 Mann-Whitney test for interaction between Reference position and control vs. dyslexics,  $z = 3$ ,  $P$   
 538  $< 0.005$ ).

539

## 540 **Discussion**

### 541 *Summary of results*

542 We dissociated the factors underlying discrimination performance into factors that stem from  
543 internal noise within a trial and those that stem from context; i.e., the stimulus statistics. We  
544 found that the context effects were significantly and substantially larger in the population of  
545 adequate readers, compared to dyslexics. When calculating the optimal weighting of previous  
546 trials, given the within trial noise and the stimulus statistics, we found that dyslexics' but not  
547 controls' weighting was indeed significantly lower than optimal. Finally, to tap dyslexics'  
548 specific difficulty in adequately weighting previous trials, we recorded ERPs. These recordings  
549 suggested that dyslexics' perceptual difficulties are associated with inadequate automatic  
550 updating-and-integrating of the context of the experiment with their current stimulus response, as  
551 observed specifically for the first tone in the pair.

552 Dyslexics' specific pattern of reduced sensitivity to the first tone in the pair, as suggested by the  
553 IMM model and observed in the ERP measures, also yielded non-intuitive predictions for a novel  
554 protocol that motivated the last experiment. Here the reference tone was presented either as the  
555 first or as the second tone. The findings showed that dyslexics' difficulties were specific to *Ref*  
556 *1<sup>st</sup>* trials.

557 We interpret all these results as an indication that dyslexics (but not controls) under-weigh  
558 history in perceptual decisions. However, dyslexics' weighting of history could alternatively be  
559 close to optimal while their deficit could be associated with increased memory noise (a  
560 possibility that goes beyond the IMM, since it requires additional assumptions). In that case,

561 increasing the weight of previous trials may not enhance their performance since it will also  
562 increase the memory noise.

563

#### 564 *Relation to previous studies of dyslexia*

565 The IMM is an extended formalization of the anchoring hypothesis of dyslexia. This theory was  
566 motivated by the observation that controls' better performance in psychoacoustic tasks  
567 (McAnally and Stein, 1996; Witton et al., 1998; Ramus et al., 2003; Ahissar et al., 2006; Ahissar,  
568 2007) and in speech discrimination (McArthur and Bishop, 2005; Ahissar et al., 2006; Boets et  
569 al., 2007) is restricted, to a large extent, to experiments in which a single reference stimulus or a  
570 small range of reference stimuli are utilized (Ahissar et al., 2006; Ahissar, 2007; Chandrasekaran  
571 et al., 2009; Banai and Ahissar, 2010; Oganian and Ahissar, 2012). The theory posits that  
572 repeated stimuli serve as an anchor, and thus boost performance when these stimuli are  
573 subsequently used. According to this theory, the ability to track such simple regularities is  
574 deficient in dyslexia.

575 The IMM presented here proposes a specific, well-defined computation that is impaired in  
576 dyslexics' incorporation of stimulus statistics. As such, the model specifies the conditions where  
577 incorporating previous trials is expected to improve perception and those where it is expected to  
578 hamper perception. Thus, unlike the intuitive anchoring hypothesis, stimulus repetition is not  
579 necessary (e.g. *Bias+* trials in a protocol with no reference), and may even not be beneficial (e.g.  
580 *Ref 2<sup>nd</sup>* trials in the reference interleaved protocol). The IMM predicts that dyslexics will only  
581 perform worse than controls on the trials that benefit from stimulus statistics.

582 The IMM assumes that the stimulus statistics are continuously learned and utilized. We found  
583 that this was indeed the case for controls and only to a lesser extent for dyslexics. The ERP

584 recordings further illustrated the analog nature of the automatic tracking mechanisms. The  
585 traditional ERP measure of automatic tracking of sounds, the mismatch negativity (MMN)  
586 component, is sensitive to the violation of repetition, and is studied in the context of oddball  
587 paradigms (Näätänen et al., 1978). The MMN component is often smaller among Dyslexics  
588 (Baldeweg et al., 1999; Kujala et al., 2003; Bishop, 2007). The findings here show that controls’  
589 automatic ERP response is parametrically sensitive to the distance of the stimulus from the peak  
590 of the stimulus distribution in previous trials. No such sensitivity was found in the dyslexic  
591 population.

592 The anchoring hypothesis and its computational implementation are inconsistent with the  
593 hypothesis that poor phonological representations are the core deficit in Dyslexia (e.g. Snowling,  
594 2000) for at least two reasons. Not only did we find difficulties in the processing of non-  
595 phonological stimuli, but in the computational framework, dyslexics’ main difficulty lay in poor  
596 usage of context. Specifically they used an overly low  $\gamma$  given their somewhat higher  $\tau$ .

597 However, our computational model is tightly related to hypotheses that associate dyslexics’  
598 difficulties with a failure to make effective predictions that can facilitate task performance  
599 (“predictive coding”, Díaz et al., 2012). However it is also compatible with hypotheses that  
600 dyslexics are less resilient to external noise (the “noise exclusion hypothesis”; e.g. Sperling et al.,  
601 2005, 2006; Beattie et al., 2011; Conlon et al., 2012; Partanen et al., 2012). According to the  
602 Bayesian framework underpinning the IMM, the prior information is utilized to compensate for  
603 the noise in the representation of the stimuli. We found that dyslexics do not properly adjust the  
604 weight of previous trials to the level of internal noise (Fig. 4). Functionally, this results in  
605 reduced noise exclusion. However, putting this broad concept in a computational framework  
606 leads to a counter-intuitive prediction: when the context is compromising (e.g. *Bias*- like

607 conditions leading to disruptive predictions), dyslexics should not do worse and may even do  
608 better than controls since this mechanism for “noise exclusion” is biased by the prior statistics.

609 Other studies have suggested that dyslexics’ implicit sequence learning is impaired (e.g. Vicari  
610 et al., 2003; Stoodley et al., 2006; Jiménez-Fernández et al., 2011). This phrasing is very broad.  
611 For example, it is not clear whether the representation of syllables should be intact, while the  
612 representation of words, which are perhaps formed by implicit sequential learning (conditional  
613 probabilities between adjacent syllables; Saffran et al., 1996) should be impaired. Our  
614 computational model assumes poor incorporation of basic attributes (zero-order statistics), as  
615 observed by the poor usage of the mean frequency of the experiment. It predicts that the same  
616 deficit may lead to reduced sensitivity to the prevalence of single syllables.

617 Other studies (Ramus and Szenkovits, 2008; Boets et al., 2013; Ramus, 2014) have proposed  
618 that phonological representations remain intact, but that dyslexics’ access to these  
619 representations is inefficient, perhaps due to impaired connectivity between the superior  
620 temporal areas which encode auditory stimuli and the frontal areas (e.g. Broca) which utilize  
621 them. This hypothesis assumes a clear distinction between representations and access, though it  
622 does not specify what “access” is, and hence which retrieval conditions should pose difficulties  
623 (e.g. whether implicit priming should be impaired). Our own perspective, as described above, is  
624 that perception is never devoid of context. Ease of retrieval is heavily affected by the availability  
625 of adequate predictions, which can substantially facilitate the process. Thus, difficulty in  
626 utilizing priors may impair the efficiency of retrieval. Nevertheless, the nature of retrieval  
627 processes in different behavioral contexts is far from being understood.

628 Recently, it has been shown that a hierarchical model of perception is able to reconstruct or  
629 decode the dynamics underlying generated series of stimuli (Yildiz et al., 2013). Our

630 observations may perhaps be interpreted within this framework, and suggest that dyslexics'  
631 deficit resides in the higher and slower level of the hierarchy, which is characterized by larger  
632 time constants, or in their impaired communication with lower levels (Boets et al., 2013). The  
633 slower dynamics in this higher level are able to track cumulating evidence and form a prior based  
634 on the underlying statistics of the stimuli. In turn, these predictions are used to modulate the  
635 lower levels of the hierarchy to better match the upcoming stimuli and the requirements of the  
636 task. This coincides with data showing that among dyslexics, task related top-down modulation  
637 is impaired (Díaz et al., 2012).

638

### 639 *Implications, limits and future directions*

640 We posited that inadequate usage of priors in the context of spoken or written language underlies  
641 dyslexics' reading deficit. This generalization is based on the fact that proficient reading of  
642 single words and even pseudo words, which are impaired in dyslexia, heavily relies on priors  
643 related to sound sequences (e.g. phonological, morphological and orthographic; see Norris,  
644 2013). In fact, dyslexics' reading of familiar words is more serial (van der Leij and van Daal,  
645 1999; Ziegler et al., 2003; Zoccolotti et al., 2005; Martens and de Jong, 2006), and their "visual  
646 word form area", an area of reading expertise that develops in parallel to readers' gradual  
647 reliance on word priors, i.e. word familiarity, is not adequately developed (Paulesu et al., 2001;  
648 Shaywitz et al., 2002; McCandliss et al., 2003).

649 However, even within the framework of the simple IMM there are open questions. First, we  
650 also found a group difference for within-trial noise ( $\uparrow$ ), which we did not expect, and should be  
651 further investigated. Additionally, it is unclear which dimensions of the priors are impaired  
652 besides frequency, e.g. intervals (Banai and Ahissar, 2006), or frequency changes in time

653 (Goswami et al., 2011), and at which time scales (the scale of phonemes, syllables, words or  
654 phrases). Moreover, dyslexics' deficit could also include other modalities, such as the spatial  
655 distribution of visual stimuli (Moore et al., 2011; Franceschini et al., 2012). A better  
656 understanding of these features is particularly important when designing novel training  
657 procedures to improve dyslexics' reading skills.

658

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662

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